ABSTRACT

If you've ever seen a box-and-whisker plot you were probably unimpressed. It lives up to its name, providing a basic visualization of the distribution of an outcome: the interquartile range (the box), the minimum and maximum (the whiskers), the median, and maybe a few outliers if you're (un)lucky. Enter the violin plot. This data visualization technique harnesses density estimates to describe the outcome’s distribution. In other words the violin plot widens around larger clusters of values (the upper and lower bouts of a violin) and narrows around smaller clusters (the waist of the violin), delivering a nuanced visualization of an outcome. With the power of SAS/GRAPH®, the savvy SAS® programmer can reproduce the statistics of the box-and-whisker plot while offering improved data visualization through the addition of the probability density ‘violin’ curve. This paper covers various SAS techniques required to produce violin plots.

INTRODUCTION

The box-and-whisker plot is a basic data visualization which with a little SAS magic can be improved drastically. The SAS programmer needs a few tools to round those hard corners. All data visualizations begin with the underlying data. Throughout this paper the dataset in reference is SASHELP.CARS, which contains qualitative and quantitative data on a number of vehicles. The idea for this paper comes from Sanjay Matange’s blog on violin plots.

The primary purpose of this paper is to illustrate similarities and differences between the box-and-whisker plot and the violin plot. Secondly I will discuss augmentations to the violin plot which provide additional information about the data. Producing a violin plot in SAS requires kernel density estimates, descriptive statistics, some data manipulation, and PROC SGPANEL, and each will be thoroughly explained.

THE BOX-AND-WHISKER PLOT

The box-and-whisker plot gives a quick outline of the distribution of continuous data. It’s a visualization of the five-number summary, i.e. the sample minimum, first quartile, median, third quartile, and sample maximum. Figure 1 displays an example of the box-and-whisker plot with horsepower as the outcome, continent of origin as the group comparison, and number of cylinders as the panel comparison.
Figure 1. Box-and-Whisker Plots

This plot visualizes the distribution of horsepower by number of cylinders and continent of origin. Each solid box encompasses all points between the first and third quartiles, otherwise known as the interquartile range. The "whiskers" encompass all points inside 1.5x the interquartile range. Points outside the interquartile range are considered outliers for the purposes of this plot. The following code will produce this plot:

```plaintext
proc sort
  data = sashelp.cars (where = (cylinders in (4 6 8)));
  by Cylinders Origin Horsepower;
run;

proc sgpanel
  data = cars;
  panelby Cylinders / novarname
    rows = 1;
  vbox Horsepower /
    group = Origin;
run;
```

It's pretty basic and I know we can do better.

**THE VIOLIN PLOT**

The violin plot is a box plot with a kernel density plot instead of a box. You might call it an outside-the-box plot. "In
statistics, kernel density estimation (KDE) is a non-parametric way to estimate the probability density function of a random variable” (“Kernel Density Estimation,” 2016, para. 1). Don’t let that scare you away. SAS makes KDE easy and besides, KDE is beyond the scope of this paper.

**Figure 2. Violin Plots**

These violin plots should look pretty familiar. They represent the same range on the y-axis as the box-and-whisker plots, which makes sense because the underlying data are the same. The similarities begin to fade upon further examination. Where the box-and-whisker plot represents a rigid interquartile range the violin plot provides a more nuanced visualization of the heart of the distribution. In some cases the “center” of the distribution is immediately apparent, as in American 4-cylinder vehicles. In other cases it’s not so apparent, as in the somewhat bimodal American 8-cylinder vehicles.

At this stage the box-and-whisker plot affords more insight into the data: the quartiles and the mean. Let’s add in these statistics:
Figure 3. Violin Plots with Quartiles and Mean

The violin plot is quickly catching up with the tried-and-true box-and-whisker plot. The small diamonds represent the first and third quartiles, the large black diamond represents the median, and the large yellow diamond represents the mean. This plot would be a bit more interesting and accessible if we color-coded the quartiles rather than placed symbols.
Figure 4. Violin Plots with Color-coded Quartiles and Mean

Not too shabby. We’ve reproduced the statistics represented in the box-and-whisker plot, namely the quartiles and the mean. With the exception of the “outliers” outside 1.5x the interquartile range these violin plots have got it all. However, perhaps the data analyst would like to see the data points which make up the distribution and further throw in some trend lines between the medians. In Figure 5 we restructure the plot and add jittered data points and trend lines.
Elevate Your Graphics Game: Violin Plots, continued

Figure 5. Violin Plots with Jittered Points and Median Trend Lines

With the restructuring and the median trend line we see a clear positive trend between number of cylinders and horsepower. The jittered data points make apparent “true” outliers.

PREPARING THE DATA

We begin with SASHELP.CARS which contains a continuous variable, horsepower, and two categorical variables, number of cylinders and continent of origin. This dataset will inform our kernel density estimation, descriptive statistics, and jittered points. To produce the KDEs we call PROC KDE:

```sas
proc sort
   data = SASHELP.CARS (where = (cylinders in (4 6 8)))
   out = cars;
   by Origin Cylinders Horsepower;
proc kde
   data = cars;
   by Origin Cylinders;
   univar Horsepower / noprint
      out = KDE;
run;
```

PROC KDE calculates the density of the distribution along the entire range of horsepower, which we use to paint the violins. One can think of KDE in the same context as ultra-granular histograms. The density values are the bins and in order to suss a violin shape out of them they need to be mirrored, i.e. negated in a separate variable. Next up are the descriptive statistics:
Everyone loves PROC MEANS and it serves its purpose competently. Here we calculate the mean and quartiles of each combination of continent of origin and number of cylinders. Finally we combine our original data points with the kernel density estimates and descriptive statistics for one Frankenstein of an input dataset.

**VISUALIZING THE DATA**

If PROC KDE and PROC MEANS produce our paint, then our paintbrush is PROC SGPANEL. First we'll apply a base coat with the BAND statement:

```sas
proc spanel nocycleattrs noautolegend
  data = carsKDEmeans;
  panelby
    Origin / novarname
    rows = 1;
  band
    y = yBand
    lower = lowerBand
    upper = upperBand / fill outline
    group = quartile
    lineattrs = (pattern = solid color = black);
run;
```

The BAND statement takes three inputs: an x- or a y-value, and a lower and upper bound from the opposing axis. In our example horsepower is plots vertically on the y-axis. Therefore our kernel density estimates and their mirrors, or negated values, plot horizontally on the x-axis. Hello violin plots! The group option on the BAND statement colors each quartile individually.

The rest is easy. SCATTER statements plot the jittered data points and descriptive statistics, and a SERIES statement plots the trend line:

```sas
scatter
  x = jitteredCylinders
  y = Horsepower /
  markerattrs = (symbol = circle size = 6px color = black);
scatter
  x = Cylinders
  y = mean /
  markerattrs = (symbol = diamondFilled size = 9px color = yellow);
```
Elevate Your Graphics Game: Violin Plots, continued

```sas
series
  x = Cylinders
  y = median /
      lineattrs = (color = red
                   thickness = 2px);
scatter
  x = Cylinders
  y = median /
      markerattrs = (symbol = circleFilled
                      size = 9px
                      color = red);
run;
```

And there you have it, a violin plot with jittered data points, descriptive statistics, and trend lines.

**THE MACRO CALL**

The macro really only requires an input dataset and an outcome variable; everything else is for added effect:

```sas
%include 'violinPlot.sas';
%violinPlot
  /*REQUIRED*/
  (data = cars /*input dataset*/
   ,outcomeVar = Horsepower /*continuous outcome variable*/
   /*optional*/
   ,groupVar = Cylinders /*categorical grouping variable*/
   ,panelVar = Origin /*categorical paneling variable*/
   ,byVar = /*categorical BY variable*/
   ,widthMultiplier = .1 /*kernel density width coefficient*/
   ,jitterYN = Yes /*display jittered data points*/
   ,quartileYN = Yes /*display color-coded quartiles*/
   ,quartileSymbolsYN = No /*display quartiles as symbols*/
   ,meanYN = Yes /*display means*/
   ,trendLineYN = Yes /*display a trend line*/
   ,trendStatistic = Median /*trend line statistic*/
  );
```

**CONCLUSION**

The box-and-whisker plot visualizes the distribution of a continuous variable fairly primitively. With kernel density estimates and PROC SGPANEL the SAS programmer can generate a far more nuanced and informative graphic. The macro `%violinPlot` allows the production of simple, quick, and professional violin plots from the SAS environment.

**REFERENCES**


ACKNOWLEDGMENTS

I’d like to thank Tee Bahnson for pointing me to Sanjay Matange’s work and for providing guidance on this project. Without Mr. Matange’s original idea I would probably still be producing box plots so he deserves a big thank you.

RECOMMENDED READING

- https://github.com/RhoInc/sas-violinPlot
- https://en.wikipedia.org/wiki/Box_plot
- https://en.wikipedia.org/wiki/Five-number_summary

CONTACT INFORMATION

Your comments and questions are valued and encouraged. Contact the author at:

Name: Spencer Childress  
Enterprise: Rho, Inc.  
Address: 6330 Quadrangle Drive  
City, State ZIP: Chapel Hill, NC 27517  
Work Phone: 919 595 6638  
Fax: 919 408 0999  
E-mail: spencer_childress@rhoworld.com  
Web: https://github.com/samussiah  
Twitter: https://twitter.com/samussiah

SAS and all other SAS Institute Inc. product or service names are registered trademarks or trademarks of SAS Institute Inc. in the USA and other countries. ® indicates USA registration.

Other brand and product names are trademarks of their respective companies.